Tits buildings and fixed points of decomposition spaces

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The space of decompositions of complex n-space into proper orthogonal decompositions has a natural action of the unitary group U(n), and makes an appearance in M. Weiss's orthogonal calculus, among other places. Until recently, relatively little has been known about its equivariant homotopy type. I will describe how the Tits buildings for the general linear group and the symplectic group make an important appearance in the fixed point sets of certain p-toral subgroups of U(n).